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## Chapter <br> Fair Game Review

Simplify the expression. Explain each step.

1. $2+(5+y)$
2. $(c+1)+9$
3. $(2.3+n)+1.4$
4. $7+(d+5)$
5. $10(7 t)$
6. $8(4 k)$
$\qquad$
$\qquad$

## Chapter 1 <br> Fair Game Review (continued)

7. $13 \bullet 0 \bullet p$
8. $7 \bullet z \bullet 0$

## 9. $2.5 \bullet w \bullet 1$

10. $1 \bullet x \bullet 19$
11. $(t+3)+0$
12. $0+(g+4)$
$\qquad$
1.1

## Integers and Absolute Value

For use with Activity 1.1
Essential Question How can you use integers to represent the velocity and the speed of an object?

On these three pages, you will investigate vertical motion (up or down).

- Speed tells how fast an object is moving, but it does not tell the direction.
- Velocity tells how fast an object is moving, and it also tells the direction.

When velocity is positive, the object is moving up.
When velocity if negative, the object is moving down.

## 1 ACTIVITY: Falling Parachute

Work with a partner. You are gliding to the ground wearing a parachute. The table shows your height above the ground at different times.

| Time (seconds) | 0 | 1 | 2 | 3 |
| :--- | :---: | :---: | :---: | :---: |
| Height (feet) | 90 | 75 | 60 | 45 |

a. Describe the pattern in the table. How many feet do you move each second? After how many seconds will you land on the ground?
b. What integer represents your speed? Give the units.
c. Do you think your velocity should be represented by a positive or negative integer? Explain your reasoning.
d. What integer represents your velocity? Give the units.
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### 1.1 Integers and Absolute Value (continued)

## 2 ACTIVITY: Rising Balloons

Work with a partner. You release a group of balloons. The table shows the height of the balloons above the ground at different times.

| Time (seconds) | 0 | 1 | 2 | 3 |
| :--- | :---: | :---: | :---: | :---: |
| Height (feet) | 8 | 12 | 16 | 20 |

a. Describe the pattern in the table. How many feet do the balloons move each second? After how many seconds will the balloons be at a height of 40 feet?
b. What integer represents the speed of the balloons? Give the units.
c. Do you think the velocity of the balloons should be represented by a positive or negative integer? Explain your reasoning.
d. What integer represents the velocity of the balloons? Give the units.

3 ACTIVITY: Firework Parachute

Work with a partner. The table shows the height of a firework's parachute above the ground at different times.
a. Describe the pattern in the table. How many feet does the parachute move each second?

| Time (seconds) | Height (feet) |
| :---: | :---: |
| 0 | 480 |
| 1 | 360 |
| 2 | 240 |
| 3 | 120 |
| 4 | 0 |

b. What integer represents the speed of the parachute? What integer represents the velocity? How are these integers similar in their relation to 0 on a number line?
$\qquad$

### 1.1 Integers and Absolute Value (continued)

## Inductive Reasoning

4. Complete the table.

| Velocity (feet per second) | -14 | 20 | -2 | 0 | 25 | -15 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Speed (feet per second) |  |  |  |  |  |  |

5. Find two different velocities for which the speed is 16 feet per second.
6. Which number is greater: -4 or 3 ? Use a number line to explain your reasoning.

7. One object has a velocity of -4 feet per second. Another object has a velocity of 3 feet per second. Which object has the greater speed? Explain your answer.
8. IN YOUR OWN WORDS How can you use integers to represent the velocity and the speed of an object?

## What Is Your Answer?

9. LOGIC In this lesson, you will study absolute value. Here are some examples:

Absolute value of $|-16|=16 \quad$ Absolute value of $|16|=16$
Absolute value of $|0|=0$
Absolute value of $|-2|=2$

Which of the following is a true statement? Explain your reasoning.

$$
\mid \text { velocity } \mid=\text { speed } \quad \mid \text { speed } \mid=\text { velocity }
$$

$\qquad$
$\qquad$

Find the absolute value.

1. $|-1|$
2. $|-14|$
3. $|0|$
4. $|6|$

Complete the statement using <, >, or $=$.
5. $6 \_|-2|$
6. $-7 \_|-8|$
7. $|-9| \_5$
8. $|-2| \_2$

Order the values from least to greatest.
9. $4,|7|,-1,|-3|,-4$
10. $|2|,-3,|-5|,-1,6$
11. You download 12 new songs to your MP3 player. Then you delete 5 old songs. Write each amount as an integer.
$\qquad$
1.2 Adding Integers

For use with Activity 1.2
Essential Question Is the sum of two integers positive, negative, or zero? How can you tell?

1 ACTIVITY: Adding Integers with the Same Sign
Work with a partner. Draw a picture to show how you use integer counters to find $-4+(-3)$.
$-4+(-3)=$ $\qquad$

2 ACTIVITY: Adding Integers with Different Signs
Work with a partner. Draw a picture to show how you use integer counters to find $\mathbf{- 3}+2$.
$-3+2=$ $\qquad$

3 ACTIVITY: Adding Integers with Different Signs
Work with a partner. Show how to use a number line to find $5+(-3)$.

$5+(-3)=$ $\qquad$
$\qquad$
1.2 Adding Integers (continued)

4 ACTIVITY: Adding Integers with Different Signs
Work with a partner. Write the addition expression shown. Then find the sum.
How are the integers in the expression related to 0 on a number line?


## Inductive Reasoning

Work with a partner. Use integer counters or a number line to complete the table.

1

| Exercise | Type of Sum | Sum | Sum: Positive, <br> Negative, or Zero |
| :---: | :---: | :---: | :---: |
| 5. $-4+(-3)$ |  |  |  |
| 6. $-3+2$ |  |  |  |
| 7. $5+(-3)$ |  |  |  |
| 8. $7+(-7)$ |  |  |  |
| 9. $2+4$ |  |  |  |
| 10. $-6+(-2)$ |  |  |  |
| 11. $-5+9$ |  |  |  |
| 12. $15+(-9)$ |  |  |  |
| 13. $-10+10$ |  |  |  |
| 14. $-6+(-6)$ |  |  |  |
| 15. $13+(-13)$ |  |  |  |

$\qquad$
1.2 Adding Integers (continued)

## What Is Your Answer?

16. IN YOUR OWN WORDS Is the sum of two integers positive, negative, or zero? How can you tell?
17. STRUCTURE Write a general rule for adding
a. two integers with the same sign.
b. two integers with different signs.
c. two integers that vary in sign.
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$\qquad$

## Practice

For use after Lesson 1.2
Add.

1. $-9+2$
2. $5+(-5)$
3. $-12+(-6)$
4. $-10+19+5$
5. $-11+(-20)+9$
6. $-7+7+(-8)$

## Use mental math to solve the equation.

7. $x+(-5)=4$
8. $y+6=-2$
9. $-10=-7+z$
10. The table shows the change in your hair length over a year.

| Month | January | February | August | September | December |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Change in hair <br> length (inches) | 2 | -1 | 3 | -4 | 3 |

a. What is the total change in your hair length at the end of the year?
b. Is your hair longer in January or December? Explain your reasoning.
c. When is your hair the longest? Explain your reasoning.
$\qquad$
1.3

Subtracting Integers
For use with Activity 1.3
Essential Question How are adding integers and subtracting integers related?

1 ACTIVITY: Subtracting Integers
Work with a partner. Draw a picture to show how you use integer counters to find 4-2.
$4-2=$ $\qquad$

2 ACTIVITY: Adding Integers
Work with a partner. Draw a picture to show how you use integer counters to find $4+(-2)$.
$4+(-2)=$ $\qquad$
3 ACTIVITY: Subtracting Integers
Work with a partner. Show how to use a number line to find -3-1.

$-3-1=$ $\qquad$
$\qquad$
$\qquad$
1.3 Subtracting Integers (continued)

4 ACTIVITY: Adding Integers
Work with a partner. Write the addition expression shown. Then find the sum.


## Inductive Reasoning

Work with a partner. Use integer counters or a number line to complete the table.

| Exercise | Operation: Add or Subtract | Answer |  |
| :---: | :---: | :---: | :---: |
| 1. | $5.4-2$ |  |  |
| 2 3 | 6. $4+(-2)$ |  |  |
| 4 | 7. $-3-1$ |  |  |
| 8. $-3+(-1)$ |  |  |  |
| 9. $3-8$ |  |  |  |
| 10. $3+(-8)$ |  |  |  |
| 11. $9-13$ |  |  |  |
| 12. $9+(-13)$ |  |  |  |
| 13. $-6-(-3)$ |  |  |  |
| 14. $-6+3$ |  |  |  |
| 15. $-5-(-12)$ |  |  |  |
| 16. $-5+12$ |  |  |  |

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### 1.3 Subtracting Integers (continued)

## What Is Your Answer?

17. IN YOUR OWN WORDS How are adding integers and subtracting integers related?
18. STRUCTURE Write a general rule for subtracting integers.
19. Use a number line to find the value of the expression $-4+4-9$. What property can you use to make your calculation easier? Explain.

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$\qquad$
1.3

## Practice

For use after Lesson 1.3
Subtract.

1. $3-8$
2. $6-(-7)$
3. $-10-9$
4. $-5-(-4)$

## Evaluate the expression.

5. $11-(-2)+14$
6. $-16-(-12)+(-8)$
7. $6-17-4$

Use mental math to solve the equation.
8. $6-x=10$
9. $y-(-10)=2$
10. $z-17=-14$
11. You begin a hike in Death Valley, California, at an elevation of -86 meters.

You hike to a point of elevation at 45 meters. What is your change in elevation?
12. You sell T-shirts for a fundraiser. It costs $\$ 112$ to have the T -shirts made.

You make $\$ 98$ in sales. What is your profit?
$\qquad$
1.4

## Multiplying Integers

For use with Activity 1.4
Essential Question Is the product of two integers positive, negative, or zero? How can you tell?

## 1 ACTIVITY: Multiplying Integers with the Same Sign

Work with a partner. Use repeated addition to find 3 • 2.
Recall that multiplication is repeated addition. $3 \bullet 2$ means to add 3 groups of 2.
$3 \cdot 2=$ $\qquad$

## 2 ACTIVITY: Multiplying Integers with Different Signs

Work with a partner. Use repeated addition to find $3 \bullet(-2)$.
$3 \cdot(-2)=$ $\qquad$

3 ACTIVITY: Multiplying Integers with Different Signs
Work with a partner. Use a table to find $\mathbf{- 3} \bullet 2$.
Describe the pattern of the products in the table. Then complete the table.

| $2 \bullet 2=$ |
| ---: | :--- |
| $1 \bullet 2=$ |
| $0 \bullet 2=$ |
| $-1 \bullet 2=$ |
| $-2 \bullet 2=$ |
| $-3 \bullet 2=$ |

$-3 \cdot 2=$ $\qquad$
$\qquad$
1.4 Multiplying Integers (continued)

4 ACTIVITY: Multiplying Integers with the Same Sign
Work with a partner. Use a table to find $-3 \bullet(-2)$.
Describe the pattern of the products in the table. Then complete the table.

| -3 | $\bullet$ | $=$ |
| :--- | :--- | :--- |
| -3 | $\bullet$ | $=$ |
| -3 | $\bullet$ | 1 |
| -3 | $\bullet$ | 0 |
| -3 | $\bullet$ | -1 |
| -3 | $\bullet$ | -2 |

$-3 \cdot(-2)=$ $\qquad$

## Inductive Reasoning

Work with a partner. Complete the table.

| Exercise | Type of Product | Product | Product: Positive or Negative |
| :---: | :---: | :---: | :---: |
| 5. $3 \cdot 2$ |  |  |  |
| 6. $3 \cdot(-2)$ |  |  |  |
| 7. $-3 \cdot 2$ |  |  |  |
| 8. $-3 \cdot(-2)$ |  |  |  |
| 9. $6 \cdot 3$ |  |  |  |
| 10. 2 • (-5) |  |  |  |
| 11. $-6 \cdot 5$ |  |  |  |
| 12. $-5 \cdot(-3)$ |  |  |  |

$\qquad$
1.4 Multiplying Integers (continued)

## What Is Your Answer?

13. Write two integers whose product is 0 .
14. IN YOUR OWN WORDS Is the product of two integers positive, negative, or zero? How can you tell?
15. STRUCTURE Write a general rule for multiplying
a. two integers with the same sign.
b. two integers with different signs.
$\qquad$
$\qquad$

## Practice

Multiply.

1. $8 \bullet 9$
2. $7(-7)$
3. $-10 \bullet 4$
4. $-5(-6)$
5. $12 \bullet(-1) \bullet(-2)$
6. $-10(-3)(-7)$
7. $-20 \bullet 0 \bullet(-4)$
8. $-4 \cdot 8 \cdot 3$

## Evaluate the expression.

9. $(-8)^{2}$
10. $-11^{2}$
11. $9 \bullet(-5)^{2}$
12. $(-2)^{3} \cdot(-6)$
13. You lose 5 points for every wrong answer in a trivia game. What integer represents the change in your points after answering 8 questions wrong?
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1.5

Dividing Integers
For use with Activity 1.5
Essential Question Is the quotient of two integers positive, negative, or zero? How can you tell?

1 ACTIVITY: Dividing Integers with Different Signs
Work with a partner. Draw a picture to show how you use integer counters to find $\mathbf{- 1 5} \div 3$.
$-15 \div 3=$ $\qquad$
2 ACTIVITY: Rewriting a Product as a Quotient
Work with a partner. Rewrite the product $3 \bullet 4=12$ as a quotient in two different ways.

First Way
12 is equal to 3 groups of $\qquad$ .
$12 \div 3=$ $\qquad$

## Second Way

12 is equal to 4 groups of $\qquad$ .
$12 \div 4=$ $\qquad$

3 ACTIVITY: Dividing Integers with Different Signs
Work with a partner. Rewrite the product $-3 \bullet(-4)=12$ as a quotient in two different ways. What can you conclude?

First Way
Second Way
$\qquad$
$\qquad$
1.5 Dividing Integers (continued)

4 ACTIVITY: Dividing Negative Integers
Work with a partner. Rewrite the product $3 \bullet(-4)=-12$ as a quotient in two different ways. What can you conclude?

First Way
Second Way

## Inductive Reasoning

Work with a partner. Complete the table.

| Exercise | Type of Quotient | Quotient | Quotient: Positive, <br> Negative, or Zero |  |
| :---: | :---: | :---: | :---: | :---: |
| (1) | 5. $-15 \div 3$ |  |  |  |
| 2 | 6. $12 \div 4$ |  |  |  |
| 7 $4.12 \div(-3)$ |  |  |  |  |
| 8. $-12 \div(-4)$ |  |  |  |  |
| 9. $-6 \div 2$ |  |  |  |  |
| 10. $-21 \div(-7)$ |  |  |  |  |
| 11. $10 \div(-2)$ |  |  |  |  |
| 12. $12 \div(-6)$ |  |  |  |  |
| 13. $0 \div(-15)$ |  |  |  |  |
| 14. $0 \div 4$ |  |  |  |  |

$\qquad$

### 1.5 Dividing Integers (continued)

## What Is Your Answer?

15. IN YOUR OWN WORDS Is the quotient of two integers positive, negative, or zero? How can you tell?
16. STRUCTURE Write a general rule for dividing
a. two integers with the same sign.
b. two integers with different signs.
$\qquad$
$\qquad$

## Practice

Divide, if possible.

1. $3 \div(-1)$
2. $8 \div 2$
3. $-10 \div 5$
4. $-21 \div(-7)$
5. $\frac{48}{-6}$
6. $\frac{-13}{-13}$
7. $\frac{0}{3}$
8. $\frac{-55}{11}$

## Evaluate the expression.

9. $-63 \div(-7)+6$
10. $-5-12 \div 3$
11. $-8 \cdot 7+33 \div(-11)$
12. The table shows the number of yards a football player runs in each quarter of a game. Find the mean number of yards the player runs per quarter.

| Quarter | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Yards | -2 | 14 | -18 | -6 |

